

MEM 733 Applied Optimal Control

Problem Set 2

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Consider the descent of the moon lander system:

$$\begin{aligned}\dot{h} &= v \\ \dot{v} &= -g + k \frac{u}{m} \\ \dot{m} &= -u\end{aligned}$$

The fuel flow rate u is used to steer the system to $h = 0, v = 0$. We wish to minimize the fuel used during landing, i.e.

$$J = \int_0^t u dt$$

The system is subject to the control constraint: $0 \leq u \leq c$, and the state constraint $h \geq 0$. Determine the optimal feedback control.